The fattened Davis complex and weighted L^2 -(co)homology of non-right angled Coxeter groups

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Abstract. Associated to a Coxeter system (W, S) there is a contractible simplicial complex Σ called the Davis complex. Given a positive real multiparameter q, one can define the weighted L^2 -(co)homology groups of Σ . We propose a program to compute the weighted L^2 -(co)homology of by considering a fattened version of this complex. The program proves successful provided that one can understand the weighted L^2 -(co)homology of nonspherical special subgroups of W. We then restrict our attention to Coxeter groups with $m_{st} = 3$; ∞ and apply this method to perform some computations.